• In high-speed aerodynamics, the important nondimensional parameters that we need to match are Mach number and Reynolds number.

$$M_{\infty} = \frac{U_{\infty}}{a} \qquad \qquad Re_L = \frac{\rho UL}{\mu} = \frac{UL}{\nu}$$

- Setting one of these numbers is easy.
- But if we want to keep the dynamic similarity, matching both numbers is not very straightforward.
- In order to maintain dynamic similarity, we need to change the reference pressure and temperature.
- The question is, what reference values do we use in order to match the Mach number and the Reynolds number?

 Let us start with the definition of the Mach number M and the Reynolds number Re (based on a characteristics length L),

$$M_{\infty} = \frac{U_{\infty}}{a} \qquad \qquad Re_L = \frac{\rho UL}{\mu} = \frac{UL}{\nu}$$

• And recall that the speed of sound a is defined as,

$$a = \left[\left(\frac{\partial p}{\partial \rho} \right)_S \right]^{\frac{1}{2}} = \sqrt{\gamma \frac{p}{\rho}} = \sqrt{\gamma R_g T}$$

• Therefore, the Mach number can be written as,

$$M_{\infty} = \frac{U_{\infty}}{a} = \frac{U_{\infty}}{\sqrt{\gamma(p/\rho)}} = \frac{U_{\infty}}{\sqrt{\gamma R_g T}}$$

- At this point the question is, how does temperature and pressure affect the Mach number and Reynolds number?
- Recall that the speed of sound and the dynamic viscosity are both functions of temperature.
- Also recall that the density is a function of pressure and temperature, and they can be related via a thermodynamics equation of state (i.e., the ideal gas law).
- Therefore, we can express the Mach number and the Reynolds number as follows,

$$M_{\infty} = \frac{U_{\infty}}{a(T)} \qquad \qquad Re_L = \frac{\rho(P, T)U_{\infty}L}{\mu(T)}$$

• We can now plug the Mach number equation into the Reynolds number expression by solving for the freestream velocity U_{∞} .

$$Re_L = \frac{\rho(P, T) M_\infty a(T) L}{\mu(T)}$$

• By using the definition of the speed of sound we obtain the following relationship,

$$Re_L = \frac{\rho(P, T) M_\infty \sqrt{\gamma R_g T} L}{\mu(T)}$$

• At this point we can use the ideal gas law to relate density to pressure and temperature as follows,

$$P = \rho R_g T$$

• By substituting the ideal gas law into the previous Reynolds number relation, we obtain the following equation,

$$Re_L = \frac{PM_{\infty}\sqrt{\gamma R_g T}L}{R_g T \mu(T)} = \frac{PM_{\infty}\sqrt{\gamma L}}{\sqrt{RT}\mu(T)}$$

• In this expression,

$$Re_L = \frac{PM_{\infty}\sqrt{\gamma R_g T}L}{R_g T \mu(T)} = \frac{PM_{\infty}\sqrt{\gamma L}}{\sqrt{RT}\mu(T)}$$

- We are only missing the dynamic viscosity dependence on temperature.
- This dependence can be computed using, for example, Sutherland's law,

$$\mu = \frac{C_1 T^{\frac{3}{2}}}{(T+C_2)}$$

- This expression corresponds to Sutherland's law with two coefficients.
- One of the many models available in the literature.

• At this point, we can solve for the pressure to obtain the following expression that relates the Mach number and Reynolds number,

$$P = \frac{Re_L\sqrt{RT}\mu(T)}{M_{\infty}\sqrt{\gamma}L}$$

- By choosing a reference temperature, we know everything on the right-hand side and can directly solve for P.
- Note that the temperature is given in Kelvins.

• The opposite approach is also possible, but it requires more work as we need to use an iterative method (e.g., Newton's method) to solve for T.

$$\sqrt{T}\mu(T) = \frac{PM_{\infty}\sqrt{\gamma}L}{Re_L\sqrt{R}}$$

- Either of the previous approaches are valid.
- However, the first approach is easier to implement.

- The main takeaway of this discussion is that when working with scaled models (in physical experiments or in numerical simulations) and in order to keep the dynamic similarity between the Mach number and the Reynolds number, you need to define the right temperature and pressure values.
- When conducting numerical simulations, you must know the reference pressure and temperature, and the working fluid used in the experimental facility.
 - Read carefully the experiment specifications or reference publication.
- A big advantage of numerical simulations is that there is no need to work with scaled models.
- But when comparing numerical simulations with the experimental values, you always need to respect the dynamic similarity because not necessarily the physical experiments are conducted full scale.

- NASA wind tunnel testing guide.
- https://www.nasa.gov/sites/default/files/atoms/files/nasa-2018-gftd_trifold-3-20-2019-508.pdf



Facility	Capabilities at a Glance
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Facility		Speed	Site	Reynolds Number	Test Section Size	Total Pressure	Total Temperature	Test Gas	Туре	Sample Test Capabilities
SUBSONIC SPEED RANGE										
14-by 22 Foot Subsonic Tunnel (14 x 22)		Mach 0 to 0.3 (348 fb/s)	NASA LARC	0 to 2.2 x 10 ⁶ per tt	14.5' H x 21.75' W x 50' L	Atmospheric	Amblent	Ar	Closed Circuit, open or closed test section	AC, FF, FO, GE, SC, HA, P, JET, R, SS, PMAI
20-Foot Vertical Spin Tunnel (VST)		0 to 90 tt/s	NASA Larc	0 to 0.55 x 10 ⁶ per ft	25' H x 20' W	Atmospheric	Amblent	Air	Closed-throat, annular return	FF, FO, SC, HA
9-by 15 Foot Low Speed Wind Tunnel (LSWT)		Mach 0 to 0.21	NASA Glenn	0 to 1.4 x 10 ⁶ per ft	9' H x 15' Wx 33' L	0 to 72 pst	Amblent to 550°R	Air	Atmospheric	PSP, Aero, UHB, PIN, PAN
Icing Research Tunnel (IRT)		Mach 0.05 to 0.50	NASA Glenn	0 to 3.6 x 10 ⁶ per ft	6' H x 9' W x 20' L	0 to 230 pst	Amblent to -35°	Ar	Closed Return - Atmospheric	In-flight licing tests and simulations
TRANSONIC SPEED REGIME										
Transonic Dynamics Tunnel (TDT)	Air Mode: Heavy Gas Mode:	Mach 0 to 1.2 Mach 0 to 1.2	NASA LARC	0.01 to 3.0 x 10 ⁶ per tt 0.1 to 9.6 x 10 ⁶ per tt	16' H x 16' W	0.5 psia to atmospheric	70° to 130°	Air R-134a	Closed Circuit	NE, FO, SC, R, SS
National Transonic Facility (NTF)	Air Mode: Cryogenic Mode:	Mach 0.1 to 1.05 Mach 0.1 to 1.20	NASA Larc	1 to 23 x 10 ⁶ per tt 4 to 140 x 10 ⁶ per tt	8.2' H x 8.2' W x 25' L	14.7 to 120 psia	+70° to +130° -250° to +130°	Air Nitrogen	Closed Circuit	PSP, TSP, Model Deformation Systems, SC, HA, JET, PT, SS
11-by 11 Foot Unitary Plan Transonic Wind Tunnel		Mach 0.2 to 1.45	NASA Ames	0.3 to 9.6 x 10 ⁶ per tt	11' H x 11'W x 22' L	432-4608 psta	110 ± 20°F	Ar	Closed Return	PSP, PIV, OF, IR, SI
SUPERSONIC SPEED REGIME										
4-Foot Supersonic Unitary Plan Wind Tunnel (UPWT)	Test Section 1: Test Section 2:	Mach 1.5 to 2.9 Mach 2.3 to 4.6	NASA LARC	0.5 to 11.4 x 10 ⁶ per ft 0.5 to 8.4 x 10 ⁶ per ft	4' H x 4' W x 7' L	0 to 10 atmospheres	100° to 300°	Dry Air	Closed Circuit	AT, FO, SC, HA, JET, PT, SS
9-by 7 Foot Unitary Plan Wind Tunnel		Mach 1.55 to 2.55	NASA Ames	0.9 to 5.6 x 10 ⁶ per ft	9' H x 7' W x 18' L	634-3888 psta	110 ± 20°F	Ar	Closed Return	IR, PSP, OF, ADST
10-by 10 Foot Foot Wind Tunnel		Mach 0 to 0.36, 2.0 to 3.5	NASA Glenn	0.12 to 3.4 x 10 ⁶ per ft	10' H x 10' W x 40' L	20 to 720 pst	520 to 1140°R	Ar	Open or Closed Circuit	PSP, SS, PN, PT
8-by 6 Foot Supersonic Wind Tunnel		0 to 0.1, 0.25 to 2.0	NASA Glenn	1.5 to 5.5 x 10 ⁶ per tt	8' W x 6' H x 23.5' L	100 to 1340 pst	520 to 720°R	Ar	Open or Closed Circuit, Atmospheric	PSP, SS, P
Propulsion Systems Lab		0 to 3.5, 0 to 6.0 w/ topping heater	NASA Glenn	n/a	12' x 12' x 39'	150 psig	850°F	Ar	Non Vittaled	Attitude king simulations
HYPERSONIC SPEED REGIME										
Langley Aerothermal Dynamics Laboratory (LAL)										
20-Inch Mach 6 Air Tunnei		Mach 6	NASA Larc	0.5 to 8.0 x 10 ⁶ per ti	20" H x 20.5" W	30 to 475 psia	760° to 940°R	Dry Air	Blow Down	AT, JET, TSP, PSP, High AOA, IR, High Speed Schlieren, BOS, PLIF, OII Flow
15-Inch Mach 6 High Temperature Tunnel		Mach 6	NASA LARC	0.5 to 6.0 x 10 ⁶ per tt	14.6" diameter open jet	50 to 450 psta	870°-1260° R	Dry Air	Blow Down	AT, JET, TSP, PSP, High AOA, IR, High Speed Schlieren, BOS, PLIF, Oli Flow
31-Inch Mach 10 Air Tunnel		Mach 10	NASA LARC	0.5 to 2.2 x 10 ⁶ per ti	31"Hx31"W	150 to 1450 psla	1850°R	Dry Air	Blow Down	AT, JET, TSP, PSP, High AOA, IR, High Speed Schileren, BOS, PLIF, Oli Flow
8-Foot High Temperature Tunnei (8-ft HTT)		Mach 3, 5 Mach 4, 5, and 7	NASA LaRC	0.44 to 5.09 x 10 ⁶ per ft	54.5" diameter Mach 3, 5 96" diameter Mach 4, 5, & 7	50 to 4000 psia	850° to 4000°	Ar	Blow Down	AT, P



- NASA wind tunnel testing guide. •
- https://www.nasa.gov/sites/default/files/atoms/files/nasa-2018-gftd_trifold-3-20-2019-508.pdf ٠



AFL

FO

Airfoil Testing to

Cround Wind Loads

Forced Oscillation

PAAI Propulsion Airframe

Aeroacoustic

Integration

Reterrent SG

Testing

Testing

AT

PMT

P

JET





Annolasti

Sensitive Paint

Testino

PSP Testing



SC Stability and Control HA High Angle-of-Attack Testino



PT Performance esting Jet Effects Testing



Shadowgraph Flow Visual



Specialized Test Techniques*

The following optical measurement techniques are in routine use at AETC facilities.

IR Thermography

Real-time measurement of surface temperature suitable for measuring heat flux, flow separation, and boundary layer transition location. Adaptive contrast enhancement algorithms are used to aid visualization of subtle temperature features.

Pressure/Temperature-Sensitive Paint

Provides continuous surface pressure and or temperature data using a paint containing fluorescent dyes which are sensitive to oxygen partial pressure as well as temperature Results can be integrated to determine airloads on wind tunnel models/components. Suitable for temperature mapping as well as boundary layer transition detection Works in cryogenic conditions where IR thermography is not suitable. Both steady state and dynamic (time resolved) data at up to 10 kHz can be obtained.

High-Speed Schlieren and Shadowgraph

Visualizes flow density variations including shock waves and vortex cores, Images can be recorded at up to 100 kHz, Data are processed to obtain frequency spectra of density fluctuations at arbitrary locations in the flow, or to obtain flow velocity by tracking the movement of turbules.

Background-Oriented Schlieren

Visualizes flow density variations by measuring fluctuations in the position of a speckled background. Able to access areas of the tunnel and viewing angles which traditional schlieren techniques cannot

Particle Image Velocimetry

A method for measuring velocity in a particle-seeded flow. A double pulsed laser sheet illuminates a two-dimensional particle field.

Non-Optical measurement techniques available

Advanced Force Balance

AETC facilities maintain a comprehensive inventory of balances for force and moment measurements including traditional six-component balances over a wide load range floor balances for semispan models, rotating balances for turbomachinery, and specialized balances for many unusual applications. In addition to balance services provided during AETC tests, balance loans may also be available.

Dynamic Data Systems

AETC facilities maintain high speed data systems suitable for excitation and readout of many types of unsteady pressure and force sensors and can accommodate tests requiring a large number of channels of unsteady data.

Other techniques, such as Oil-Film Interferometry, Planar Laser Induced Fluorescence, and Femtosecond laser Electronic Excitation and Tagging are also available upon request.



- A few links to wind tunnel facilities around the world:
 - <u>https://www.nasa.gov/centers/langley/news/factsheets/WindTunnel.html</u>
 - <u>https://www.nasa.gov/centers/ames/orgs/aeronautics/windtunnels/index.html</u>
 - <u>https://www.etw.de/wind-tunnel/overview</u>
 - <u>https://www.onera.fr/en/windtunnel</u>