Turbulence and CFD models: Theory and applications

Roadmap to Lecture 7

Part 7

- 1. On the closure coefficients
- 2. Galilean invariance
- 3. URANS and RANS

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- 1. On the closure coefficients
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- The coefficients used in the turbulence models do not come out of thin air.
- They have been calibrated using experiments, numerical simulations, or empirical correlations.
- During this calibration process, many assumptions are taken that sometimes might not be very realistic or hard to digest.
- Such as, local equilibrium, local isotropy, homogeneity, two-dimensional flow, fully developed flow, pure shear flow, decaying homogenous turbulence, and so on.
- Optimization methods are also being used to calibrate these coefficients.
- And more recently, data driven simulations and machine learning methods are being used for calibration of the coefficients.
- Notice that we call then coefficients and not constants.
- They certainly can be adjusted (using good judgement).

• Let us review the $\,k-\epsilon\,$ turbulence model,

$$\nabla_t k + \nabla \cdot (\bar{\mathbf{u}}k) = \tau^R : \nabla \bar{\mathbf{u}} - \epsilon + \nabla \cdot \left[\left(\nu + \frac{\nu_t}{\sigma_k} \right) \nabla k \right]$$

$$\nabla_t \epsilon + \nabla \cdot (\bar{\mathbf{u}}\epsilon) = C_{\epsilon_1} \frac{\epsilon}{k} \tau^R : \nabla \bar{\mathbf{u}} - C_{\epsilon_2} \frac{\epsilon^2}{k} + \nabla \cdot \left[\left(\nu + \frac{\nu_t}{\sigma_\epsilon} \right) \nabla \epsilon \right]$$

This model uses the following relation for the kinematic eddy viscosity,

$$\nu_t = \frac{C_\mu k^2}{\epsilon}$$

With the following closure coefficients,

$$C_{\epsilon_1} = 1.44$$
 $C_{\epsilon_2} = 1.92$ $C_{\mu} = 0.09$ $\sigma_k = 1.0$ $\sigma_{\epsilon} = 1.3$

And auxiliary relationships,

$$\omega = \frac{\epsilon}{C_{\mu}k} \qquad \qquad l = \frac{C_{\mu}k^{3/2}}{\epsilon}$$

Let us address how to calibrate the eddy viscosity coefficient C_{μ} which is used in the following eddy viscosity relation,

$$\nu_t = C_\mu \frac{k^2}{\epsilon}$$

- As we have seen, this equation is used in two-equation models.
- In the $k-\epsilon$ model, the coefficient C_μ is equal to 0.09.
- This coefficient also appears in the $k-\omega$ model, but it is called β^* instead.
- This coefficient can be calibrated using the approximation of the two-dimensional shear layer flow.
- That is, we are dealing with a simple pure shear flow, a big simplification.
- Additionally, let us assume local equilibrium which means that the ratio of production and dissipation is approximately one (his scenario usually happens far from the walls).
- However, this hypothesys is not entirely true, as this quantities are not entirely in equilibrium, even in shear flows.
- And as usual, we assume local isotropy at the level of the smallest scales.

 Talking about canonical or simplified solutions, the RANS equations for a two-dimensional boundary layer (or pure shear flow) can be written as follows,

$$\frac{\partial \overline{u}}{\partial x} + \frac{\partial \overline{v}}{\partial y} = 0$$

$$\overline{u}\frac{\partial \overline{u}}{\partial x} + \overline{v}\frac{\partial \overline{u}}{\partial y} = -\frac{1}{\rho}\frac{\partial \overline{p}}{\partial x} + \nu\frac{\partial^2 \overline{u}}{\partial y^2} + \frac{\partial}{\partial y}\left(\overline{u'v'}\right)$$

$$\frac{\partial \overline{p}}{\partial y} \approx 0$$

Where the following assumptions were taken,

$$v << u$$
 $\frac{\partial}{\partial x} << \frac{\partial}{\partial y}$ $\frac{\partial p}{\partial y} << \frac{\partial p}{\partial x}$

 Under certain conditions, these equations provide high quality solutions of turbulent flows that can be used to validate models and calibrate coefficients.

• If production is equal to dissipation, *i.e.*, $P=\epsilon$, we obtain,

$$\underbrace{\tau_{uv}\frac{\partial \overline{u}}{\partial y}}_{P} = \epsilon$$

• Using the Boussinesq hypothesis to derive T_{uv} ,

$$\tau_{uv} = -\overline{u'v'} = \nu_t \frac{\partial \overline{u}}{\partial y}$$

Combining the two previous equations, so we drop the derivative, we obtain,

$$\frac{\tau_{uv}^2}{\nu_t} = \epsilon$$

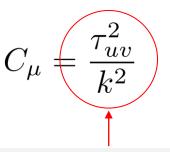
Finally, using the following relation of eddy viscosity,

$$\nu_t = C_\mu \frac{k^2}{\epsilon}$$

Together with the following relationship (that we obtained in the previous slide),

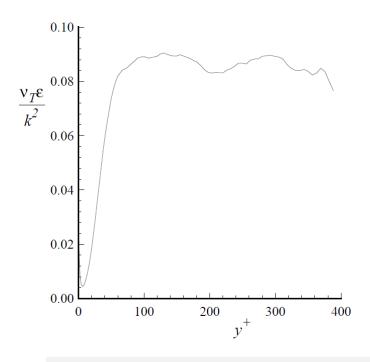
$$\frac{\tau_{uv}^2}{\nu_t} = \epsilon$$

• We obtain the following relation to estimate the eddy viscosity coefficient $\,C_{\mu}$,

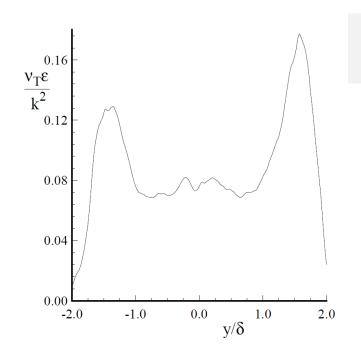


This quantity can be measured using DNS or experiments
It represents the ratio of the shear Reynolds stress to turbulent kinetic energy

• For simple shear flows the quantities k , ϵ , $u_t=-\overline{u'v'}/(\partial\overline{u}/\partial y)$, can be measured.



J. Kim, P. Moin, R. Moser. Turbulence statistics in fully developed channel flow at low Reynolds number. 1987.



M. Rogers, R. Moser. Direct simulation of a self-similar turbulent mixing layer. 1994.

In local equilibrium, $\nu_t \epsilon = \tau_{uv}^2,$

- From these results, it can be seen that the eddy viscosity coefficient $\,C_{\mu}\,$ is approximately equal to 0.09
- This is where DNS and canonical flows come in handy.

• The calibrated eddy viscosity coefficient $\,C_{\mu}\,$ can be expressed as,

$$C_{\mu} = \frac{\tau_{uv}^2}{k^2} = 0.09$$

Sometimes in the literature you will find,

$$\sqrt{C_{\mu}} = \beta_r = \frac{\tau_{uv}}{k} = 0.3$$

- Where the ratio of the Reynolds stress to turbulent kinetic energy, *i.e.*, β_r , is often referred to as Bradshaw's constant [1].
- And sometimes as to Townsend's constant [2].

- Let us address the calibration of the coefficient $C_{\epsilon 2}$.
- This coefficient can be calibrated using the hypothesis of decaying homogenous turbulence.
- In this type of flow, the mean velocity and mean velocity gradients are equal to zero, we are only modeling decay, another huge simplification.
- In this case, the governing equations can be expressed as follows,

$$\frac{\partial k}{\partial t} = -\epsilon \qquad \qquad \frac{\partial \epsilon}{\partial t} = -C_{\epsilon 2} \frac{\epsilon^2}{k}$$

Using experimental data and looking for power law solutions, an expression for $C_{\epsilon 2}$ is obtained as a function of a decay exponent, as follows,

$$k = \frac{k_0}{(t/t_0 + 1)^n}$$
 $C_{\epsilon 2} = \frac{n+1}{n}$

- Fitting experimental data, the decay coefficient n can be obtained.
- As can be seen, depending on the data, the value of the coefficient $C_{\epsilon 2}$ will vary.
- Values ranging from 1.5 to 2.2 are often found in the literature.

References:

- Let us address the coefficient $C_{\epsilon 1}$, its calibration is also related to experimental data.
- In this case, we use the assumption of homogenous shear flow, which is not often found in industrial applications.
- Under these assumptions, the governing equations can be expressed as follows,

$$\frac{\partial k}{\partial t} = P_k - \epsilon \qquad \qquad \frac{\partial \epsilon}{\partial t} = \frac{C_{\epsilon 1} P_k - C_{\epsilon 2} \epsilon}{k/\epsilon}$$

Combining these equation we can find the following relationship,

$$C_{\epsilon 1} = \frac{C_{\epsilon 2} - 1}{P_k / \epsilon} + 1$$

- By using growth rates of homogenous sheared turbulence (for the spreading rate in a plane mixing layer), we can find the coefficient $C_{\epsilon 1}$.
- Values ranging from 1.2 to 2.0 are often found in the literature.

- Let us address the coefficient σ_{ϵ} .
- This closure coefficient acts like an effective Prandtl number for dissipation diffusion and is specified to ensure the correct log-law slope of κ^{-1} (Karman constant).
- Using the previous coefficients, the value of σ_{ϵ} can be found using the following relationship,

$$\sigma_{\epsilon} = \frac{\kappa^2}{(C_{\epsilon 1} - C_{\epsilon 2})\sqrt{C_{\mu}}}$$

- This is the equation used by Jones and Launder (see references) to determine the value of the coefficient σ_{ϵ} .
- The original value obtained by Jones and Launder is equal to 1.3.
- Values ranging from 1.2 to 1.5 are often found in the literature.
- Notice that this relation can also be used to derive the value of the Karman constant κ by adjusting the value of the coefficients to produce a particular value of κ .
- This implies the use of data fitting or optimization methods.

- Let us look back at the relationship for σ_{ϵ} presented in the previous slide.
- That relationship was obtained by manipulating the solvable dissipation rate equation and using some additional relations and assumptions.
- By rearranging the relationship, we obtain the following equation,

$$\frac{\sqrt{C_{\mu}}\sigma_{\epsilon}}{\kappa^2} \left(C_{\epsilon 1} - C_{\epsilon 2} \right) = 1$$

• Using the standard coefficients of the $\,k-\epsilon\,$ model,

$$C_{\epsilon_1} = 1.44$$
 $C_{\epsilon_2} = 1.92$ $C_{\mu} = 0.09$ $\sigma_k = 1.0$ $\sigma_{\epsilon} = 1.3$

- In the left-hand side of the previous condition, we obtain a value of 1.11, showing that this constraint is reasonably well satisfied.
- Which suggests that some kind of optimization method or data drive approach could be used to calibrate all these coefficients.
- Machine learning methods are used today to calibrate turbulence models.

- Finally, let us address the coefficient σ_k .
- This term affect the effective diffusivity in the TKE equation.
- Generally speaking, there is no consensus within the turbulence community about the value of this coefficient.
- Different values can be used depending on the set of experimental data available.
- In most cases this coefficient is assumed to be one.
- In fact, we have assumed that the value of this coefficient is one.
- Values ranging from 0.8 to 1.2 are often found in the literature.
- This coefficient is usually use in the presence of thermal or mass diffusion.

• Some observations on the effect of changing the closure coefficients in the standard $k-\epsilon$ turbulence model,

Coefficient	Value	Result of Increasing Value
C_{μ}	0.09	More mixing, more shear, greater change in pressure
$C_{\epsilon 1}$	1.44	Less mixing, lower shear, smaller change in pressure
$C_{\epsilon 2}$	1.92	More mixing, more shear, greater change in pressure
σ_k	1.0	Less mixing (Prandtl-Schmidt number)
σ_ϵ	1.3	Less mixing (Turbulent Prandtl number)

$$\nabla_{t}k + \nabla \cdot (\bar{\mathbf{u}}k) = \tau^{R} : \nabla \bar{\mathbf{u}} - \epsilon + \nabla \cdot \left[\left(\nu + \frac{\nu_{t}}{\sigma_{k}} \right) \nabla k \right]$$

$$\nabla_{t}\epsilon + \nabla \cdot (\bar{\mathbf{u}}\epsilon) = C_{\epsilon_{1}} \frac{\epsilon}{k} \tau^{R} : \nabla \bar{\mathbf{u}} - C_{\epsilon_{2}} \frac{\epsilon^{2}}{k} + \nabla \cdot \left[\left(\nu + \frac{\nu_{t}}{\sigma_{\epsilon}} \right) \nabla \epsilon \right]$$

$$\nu_{t} = \frac{C_{\mu}k^{2}}{\epsilon}$$

- These observation can also be used with other variants of the $k-\epsilon$ turbulence models.
- Use with care as these are rough observations.

- All the coefficients used in all turbulence models, undergo a similar calibration process.
- We briefly discussed how to calibrate the coefficients of the standard $k-\epsilon$ turbulence model.
- The interested reader should refer to the original references of the turbulence model for a detailed description of the calibration of all coefficients.
- If you are interested in the standard $k-\epsilon$ turbulence model, these are the original references,
 - [1] B. E. Launder, D. B. Spalding. The Numerical Computation of Turbulent Flows. Computer Methods in Applied Mechanics and Engineering. 1974.
 - [2] B. E. Launder, B. I. Sharma. Application of the Energy-Dissipation Model of Turbulence to the Calculation of Flow Near a Spinning Disc. Letters in Heat and Mass Transfer. 1974.
- If you are interested in the Wilcox 1988 $k-\omega$ turbulence model,
 - [1] D. C. Wilcox. Reassessment of the Scale-Determining Equation for Advanced Turbulence Models. AIAA Journal, 1988.
 - [2] D. C. Wilcox. Turbulence Modeling for CFD. DCW Industries, 2010.
- Plus, many additional cross-references.

At this point cynics might protest:

"This is pure empiricism! How can an entirely fictional equation, plucked out of thin air, and forced, through the judicious choice of some arbitrary coefficients, to reproduce one or two laboratory results, possibly hope to anticipate the evolution of a wide range of flows?"

The extraordinary thing, however, is that, by and large, it works reasonably well, at least much better than it ought to. So perhaps there is more to

$$\nabla_t \epsilon + \nabla \cdot (\bar{\mathbf{u}}\epsilon) = C_{\epsilon_1} \frac{\epsilon}{k} \tau^R : \nabla \bar{\mathbf{u}} - C_{\epsilon_2} \frac{\epsilon^2}{k} + \nabla \cdot \left[\left(\nu + \frac{\nu_t}{\sigma_\epsilon} \right) \nabla \epsilon \right]$$

than meets the eye. Perhaps there is some underlying rationale for this equation. It turns out that there is.

P. Davidson [1]

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- 1. On the closure coefficients
- 2. Galilean invariance
- 3. URANS and RANS

- Something we all take for granted as part of our Newtonian view is that the phenomena of fluid mechanics are physically the same, regardless of what reference frame we choose to view them in.
- Any fluid flow may be described with equal validity whether the reference frame is inertial (not accelerating or rotating) or is accelerating and/or rotating.
- The Navier-Stokes equations and the general boundary conditions used with them are invariant under Galilean transformation, which means that the forms of the equations and the boundary conditions are unchanged by a transformation from one inertial frame to another.
- The fact that we can look at the equations of fluid dynamics and their related physical interpretation in different reference frames and know that they are effectively the same comes in handy in many ways.
- For example, it is basic to the similarity between wind-tunnel testing and flight.
- Just like all phenomena described by classical mechanics, the behavior of fluid flows is the same in all inertial frames.
- The idea of independence of reference frame worth a cursory look.

The Galilean transformation between two coordinated systems can be defined as follows,

$$x' = x - Vt$$

$$y' = y$$

$$z' = z$$

$$t' = t$$

The moving coordinate system (the primed notation) is moving with respect to the fix reference system (unprimed) with a velocity V (as measured in the fix system) in the x direction.

$$U'(\mathbf{x}', t') = U(\mathbf{x}, t) - V$$
$$u' = u - V$$

- A quantity that is the same in different inertial frames is said to be Galilean invariant.
- Let us transform one coordinate system to the other coordinate system.

- Let us differentiate the variable ϕ (which is in function of space **x** and time t).
- By applying the chain rule, we obtain,

$$\frac{\partial t'}{\partial x} = 0$$

$$\frac{\partial \phi}{\partial x} = \frac{\partial x'}{\partial x} \frac{\partial \phi}{\partial x'} + \frac{\partial t'}{\partial x} \frac{\partial \phi}{\partial t'} = \frac{\partial \phi}{\partial x'}$$

$$\frac{\partial x'}{\partial x} = 1$$

- Therefore, the gradient of ϕ is the same in both coordinate systems.
- The gradient is Galilean invariant.
- A similar result can be obtained for the Laplacian.

- Let us differentiate the variable ϕ (which is in function of space **x** and time t).
- By applying the chain rule, we obtain,

$$\frac{\partial t'}{\partial t} = 1$$

$$\frac{\partial \phi}{\partial t} = \frac{\partial x'}{\partial t} \frac{\partial \phi}{\partial x'} + \frac{\partial t'}{\partial t} \frac{\partial \phi}{\partial t'} = -V \frac{\partial \phi}{\partial x'} + \frac{\partial \phi}{\partial t'}$$

$$\frac{\partial x'}{\partial t} = -V$$

- Therefore, the partial time derivative of ϕ is not Galilean invariant.
- For example, the partial time derivative of velocity is not Galilean invariant.
- Also, the velocity is not Galilean invariant.

Let us apply the previous results to the material derivative,

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x}$$

Substituting and doing some algebra, we obtain,

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} = \frac{\partial \phi}{\partial t'} - V \frac{\partial \phi}{\partial x'} + u \frac{\partial \phi}{\partial x'} = \frac{\partial \phi}{\partial t'} + u' \frac{\partial \phi}{\partial x'}$$

$$\downarrow u = u' + V$$

- Notice that the terms where the velocity V appears cancel out.
- Therefore, the material derivative is Galilean invariant.

- We just showed that the velocity gradients and the material derivative are Galilean invariant.
- Whereas the velocity and its partial time derivative are not Galilean invariant.
- Other quantities that are Galilean invariant include transported scalars (such as temperature, species, concentration, and pressure), and quantities related to velocity gradients, e.g., strain rate, vorticity, and so on.
- All these operators appear in the Navier-Stokes equations; therefore, they are Galilean invariant.
- The Reynolds stress tensor modeled using the Boussinesq hypothesis is also Galilean invariant.
- Therefore, the RANS/URANS equations are Galilean invariant.

- However, the closure models are not all born Galilean invariant.
- The concept of Galilean invariance is an important tool when developing closure models.
- Models must not be sensitive to system translation, must not depend on the orientation of the system axes, and must be applicable to an accelerating or rotating system.
- The fact that a turbulence model is not Galilean invariant does not mean that it is useless. It
 only limits the model to fixed coordinate systems.
- For example, the γRe_{θ} transition model is not Galilean invariant.

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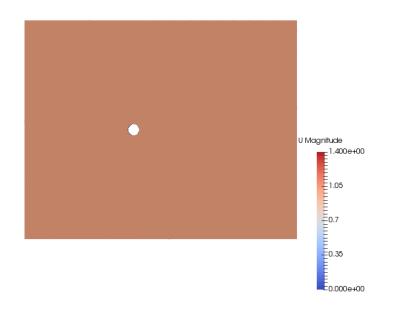
- So far, we have established that in RANS simulations we neglect the time derivative and in URANS simulations we retain the time derivative.
- But it is a little bit more complicated than that.
- The choice of the approach, RANS or URANS, strongly depends on the unsteadiness of the flow physics.
- The unsteadiness can be due the coherent vortical structures, large scale eddies, multiphase flows, external forces, boundary conditions, moving bodies, and so on.
- Have in mind that it is possible to use RANS solvers with unsteady physics.
- However, the results will be more questionable than they already are.
- Ultimately, it is up to the user to choose between RANS (steady solver) or URANS (unsteady solver).
- You must understand your physics, know your resources, and get a compromise between accuracy and computing speed.

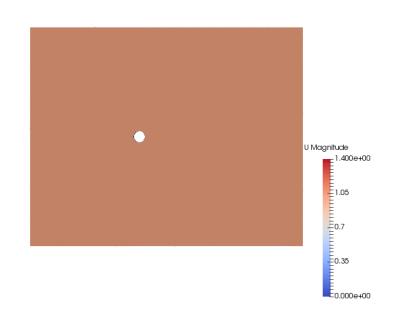
- The mean flow computed in RANS simulations can be viewed as an ensemble or time averaged field.
- Any unsteadiness inherent to the turbulent eddies is removed by the averaging process in RANS.
- Yes, the unsteadiness can be present in the steady solver, but the solution is not time accurate.
- RANS simulations implies that the resolved quantities depends only on space.
- It is important to stress that the hypothesis of steadiness is very questionable, with results that might be even more questionable.
- But if the flow is truly steady (this is the exception rather than the rule) or mildly unsteady, the steady hypothesis is acceptable.
- In many engineering applications steady solutions are acceptable and highly desirable.

- Two questions should always be asked when using RANS models,
 - How well does the steady model hypothesis capture the flow physics?
 - How accurate are the quantitative predictions obtained in the analysis?
- If you cannot answer positively the previous questions or if you know that the flow physics is strongly unsteady, it is better to use unsteady RANS (or URANS).

Flow about a circular cylinder – Re = 200 -**Unsteady physics**

Time: 0.000000 Iteration: 0.000000



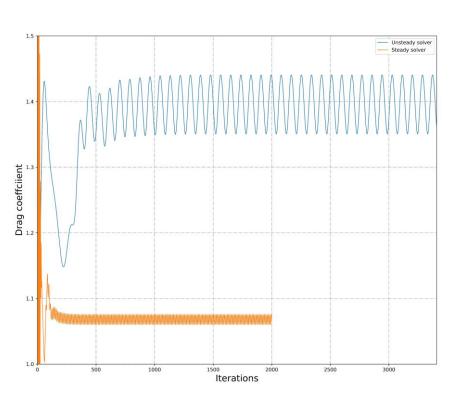


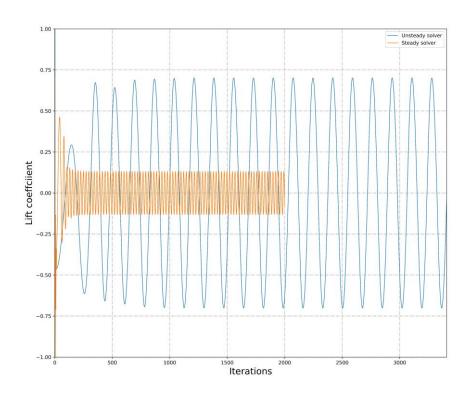
Re = 200
Unsteady physics with unsteady solver – URANS solver

Re = 200
Unsteady physics with steady solver – RANS solver

· Note that we added a non-uniform initialization to onset the instability faster.

Flow about a circular cylinder – Re = 200





Unsteady solver (URANS) and steady solver (RANS) comparison

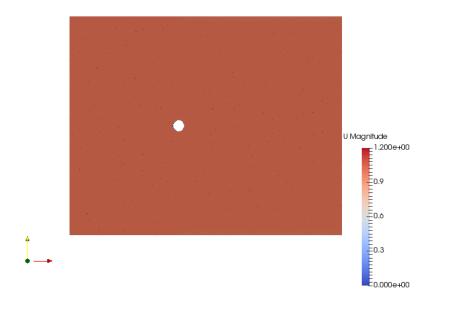
Comparison of the drag coefficient outcome

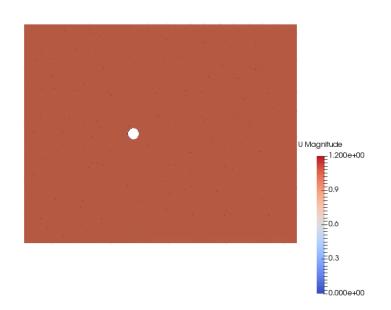
Unsteady solver (URANS) and steady solver (RANS) comparison

Comparison of the lift coefficient outcome

Flow about a circular cylinder – Re = 20 -Steady physics

Time: 0.000000 Iteration: 0.000000



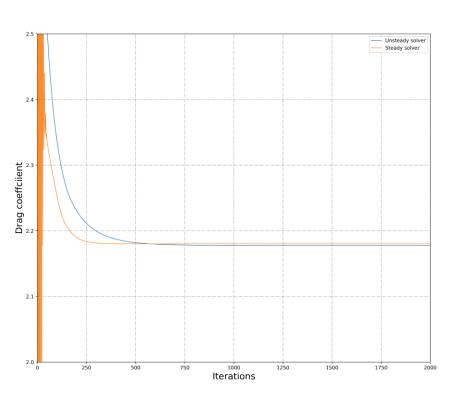


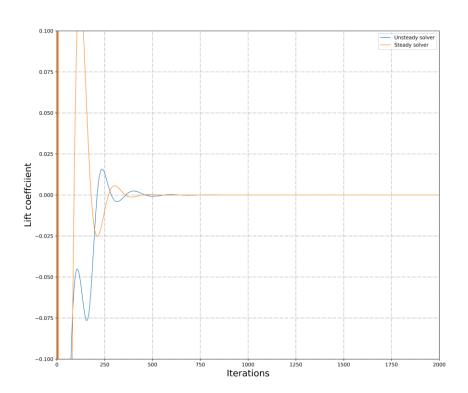
Re = 20 Steady physics with unsteady solver – URANS solver

Re = 20 **Steady physics** with **steady solver – RNAS solver**

- · Note that we added a non-uniform initialization to onset the instability faster.
- However, the instability is not present as the Reynolds number is low

Flow about a circular cylinder – Re = 200





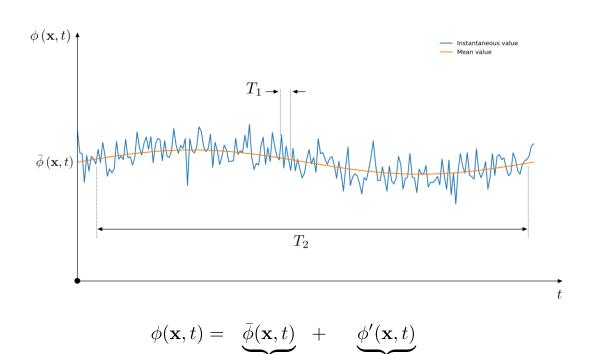
Unsteady solver and steady solver comparison

Comparison of the drag coefficient outcome

Unsteady solver and steady solver comparison

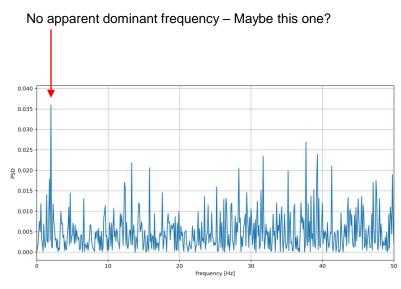
Comparison of the lift coefficient outcome

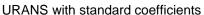
- In unsteady RANS (or URANS), the mean flow is viewed as the result of the ensemble average or time averaging over a time period must smaller than the long period oscillations present in flow field (T₂ in the figure), and larger than the instantaneous fluctuations (T₁ in the figure).
- In the figure, T₂ is a time scale characteristic of a slow variation in the flow that we do not wish to regard as belonging to the turbulence fluctuations.
- Remember, at the end of the day we do not want to solve the instantaneous fluctuations because it is too expensive.

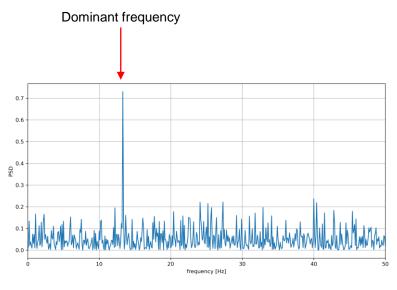


- In the previous situation, we were assuming that the time scales T₁ and T₂ exist and differ by several order of magnitude.
- But it might happen that in some situations this requirement is not satisfied.
- In such cases, the time averaging applied to the equations will remove or average these time scales.
- And this is due to the fact that there is no distinct separation between the flow unsteadiness and the turbulent fluctuations.
- This separation between the flow scales and turbulent fluctuations is known as spectral gap.
- In cases where the spectral gap is not large enough, so it is not possible to distinct between the turbulent fluctuation and the flow scales, the time averaging used in standard URANS methods will add numerical diffusion to solution, and it will underestimate/overestimate the physics of interest.
- In this situation the mean flow and the fluctuations are correlated.

- In recent years, variations of URANS models have been developed that allow for the inclusion of transient, random large-scale structures.
- Such schemes generally are based on lowering the local eddy viscosity of the method to the point that diffusion no longer suppresses instabilities.
- Such effect can also be achieved by recalibrating the coefficients of the URANS model.
- In particular, the value of the coefficient C_{μ} is often decreased (and as a results μ_t) [1, 2].
- In the figure below, we show the effect of adjusting the coefficient C_{μ} (the specific application is not important). In this case, a lower value of the coefficient adds less dissipation.





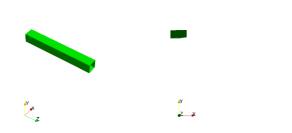


URANS with lower C_{μ}

^[1] F. Bastin, P. Lafon, S. Candel. Computation of jet mixing noise due to coherent structures: the plane jet case. J. Fluid Mech., 335, 261–304. 1997.

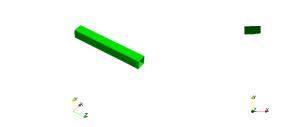
Vortex shedding past square cylinder





URANS (K-Omega SST with no wall functions) – Vortices visualized by Q-criterion

www.wolfdynamics.com/wiki/squarecil/urans2.gif



LES (Smagorinsky) – Vortices visualized by Q-criterion www.wolfdynamics.com/wiki/squarecil/les.gif

Comparison of an URANS simulation and a LES simulation.

- The quantitative results (drag coefficient and shedding frequency) are very similar in both cases.
- But qualitatively speaking, the solutions are very different.
- URANS simulations add a lot of dissipation to the solution.
- They do not resolve well the vortical structures in all directions. Particularly, in the spanwise direction (vortex stretching).
- And if there is no spectral gap between the turbulent fluctuations and the mean flow fluctuations (the vortex shedding frequency in this case), URANS will remove the mean flow fluctuations.

- Adjusting the coefficients of the URANS model, might not always be the best solution when dealing with strong unsteadiness and small spectral gaps.
- In the situations where we are interested in resolving the turbulent spectrum instead of modeling it (as in RANS/URANS), we can resort to another type of approach, namely, scale-resolving simulations or SRS.
- SRS refers to all turbulence models which resolve at least a portion of the turbulence spectrum
 in at least a part of the domain.
- Just to name a few of the approaches found in SRS:
 - Large eddy simulations (LES), detached eddy simulations (DES), scale adaptive simulation (SAS), wall-modeled LES (WMLES), hybrid URANS-LES, embedded LES (ELES), stress-blended eddy simulations (SBES).
- SRS is a field of intense research, and many new formulations continue to emerge.
- We will explore LES and DES in lecture 10.
- Have in mind that these approaches are intrinsically 3D and unsteady; therefore, computationally expensive.

The workhorse of turbulence modeling in CFD, RANS/URANS.

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 - Scale adaptive simulation (SAS).
 - Wall-modeled LES (WMLES).
 - Hybrid URANS-LES.
 - Embedded LES (ELES).
 - Stress-blended eddy simulations (SBES).
 - And many more.

- SRS is a field of intense research, and many new formulations continue to emerge.
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- The workhorse of turbulence modeling in industrial CFD, RANS/URANS.
- With a trend to move towards non-linear eddy viscosity models and algebraic Reynolds Stress models.