

13/12/2013



University of Genoa  
Faculty of Engineering

# Master Thesis in Mechanical Engineering

**DEVELOPMENT OF A TOOL FOR THE PREDICTION  
OF TRANSITION TO TURBULENCE OVER SMALL  
AIRCRAFT WINGS**

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**Co-Advisor: Ing. Christophe Favre**

**Co-Advisor: Prof. Alessandro Bottaro**

**Candidate: Marina Bruzzone**

# OUTLINE



Two phases:

- 4 months preparation with Professor Jan O. Pralits, Genoa
- 6 months internship at Daher-Socata, Aéroport de Tarbes-Lourdes



# OUTLINE

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- Introduction and Motivation
- Theory
- Methodology developed
- Test cases validation in 2D
- Test case validation in 3D
- Conclusions and Future Work

# INTRODUCTION & MOTIVATION



- Increase of aircraft efficiency to **improve the performances**.
- In aerodynamics **friction drag prediction** is important.
- Drag is directly linked **to transition and turbulence**. Laminar flow corresponds to low drag and turbulent flow to larger drag.
- Increasing the laminar flow on the wings, winglets, tail, fin and nacelles can reduce fuel **consumption of 15% (potential to save money and environment)**
- How and when a **flow** becomes **turbulent** is a classic **unsolved problem in fluid mechanics**. Simplified methods for transition prediction exist.
- Objective: Validate a **transition prediction process** on **2D** profiles and apply it on a **3D** geometry, as applied to small aircraft wings.





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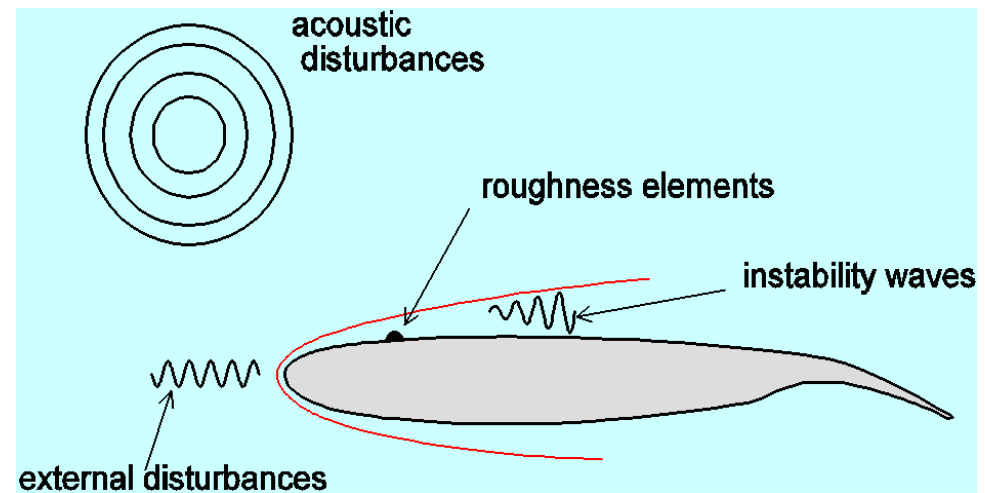
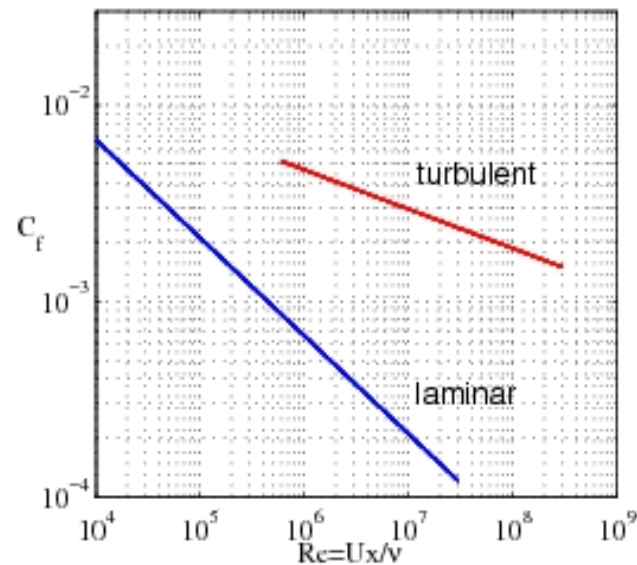
# THEORY



# THEORY

Transition is assumed to occur when the **amplitude** of small perturbations, which grow as they propagate downstream, **reaches a certain value**.

- **LAMINAR FLOW** on wings means lower drag and reduced fuel consumption
- **RECEPTIVITY**: disturbances in the free stream enter the boundary layer as unsteady fluctuations

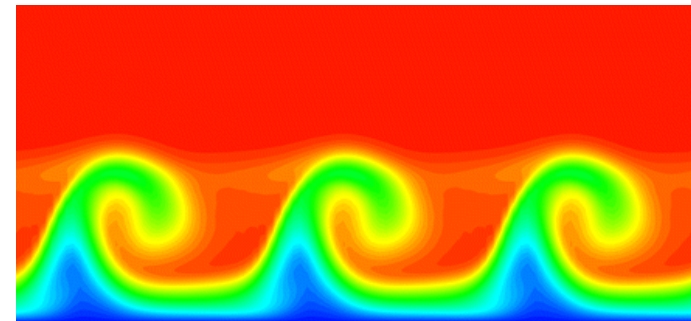
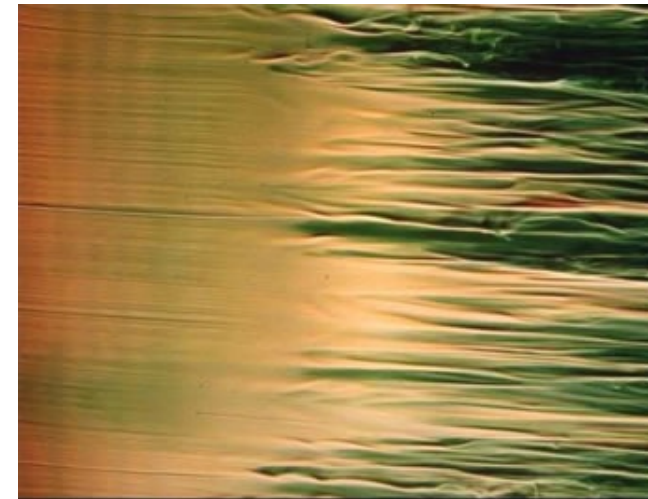


# THEORY



Due to receptivity mechanisms disturbances enter the laminar boundary layer, and might trigger unstable disturbances in the boundary layer, such as:

- **Tollmien-Schlichting waves:** (2D flows)
  - Instabilities develop as **wave-like disturbances**.
  - Their periodic form **grows exponentially**.
  - The **first stage** can be studied by **linear theory**.
  - **After** they reach a **finite amplitude** and a **random character**.
- **CrossFlow instabilities:** (3D flows)
  - Typical of 3D flow so, for instance for a **swept wing**.
  - Qualitatively the same phenomena but propagated in a **wide range of directions**
  - CF instabilities appear as **co-rotating vortices**

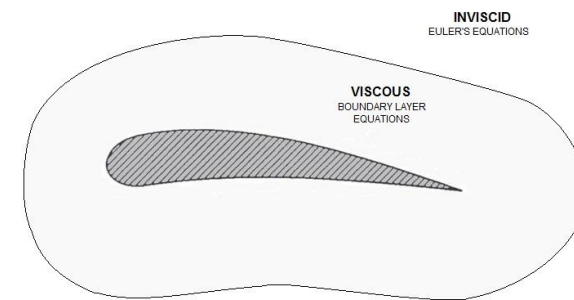
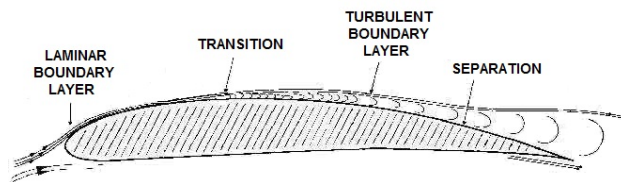


# THEORY



**Viscosity** influences a **very thin layer** in the immediate neighborhood of the solid wall.

Prandtl's idea of *boundary layer* is to divide the flow into **two regions**, the **outer one** is approximated with no viscosity and one **internal** where the **friction** must be taken into account.



- Considering variables composed by a **base flow** part and a **fluctuating** one, for
  - parallel
  - two-dimensional
  - incompressible flow

$$\vec{V} = \vec{V}_b + \vec{V}' \quad P = P_b + P'$$

- Continuity** and **Navier Stokes** equations are simplified considering:
  - Non linear terms** of disturbances can be neglected.
  - Mean flow quantities** scale is significantly bigger than the disturbances' one.

$$\frac{\partial u'}{\partial x} + \frac{\partial v'}{\partial y} + \frac{\partial w'}{\partial z} = 0$$

$$\left\{ \begin{aligned} \frac{\partial u'}{\partial t} + U \frac{\partial u'}{\partial x} + v' \frac{\partial U}{\partial y} &= -\frac{\partial p'}{\partial x} + \frac{1}{Re} \left( \frac{\partial^2 u'}{\partial x^2} + \frac{\partial^2 u'}{\partial y^2} + \frac{\partial^2 u'}{\partial z^2} \right) \\ \frac{\partial v'}{\partial t} + U \frac{\partial v'}{\partial x} &= -\frac{\partial p'}{\partial y} + \frac{1}{Re} \left( \frac{\partial^2 v'}{\partial x^2} + \frac{\partial^2 v'}{\partial y^2} + \frac{\partial^2 v'}{\partial z^2} \right) \\ \frac{\partial w'}{\partial t} + U \frac{\partial w'}{\partial x} &= -\frac{\partial p'}{\partial z} + \frac{1}{Re} \left( \frac{\partial^2 w'}{\partial x^2} + \frac{\partial^2 w'}{\partial y^2} + \frac{\partial^2 w'}{\partial z^2} \right) \end{aligned} \right.$$



# THEORY



These equations are expressed through only **two variables**:

$$v' = \tilde{v}(y)e^{i(\alpha x + \beta z - \omega t)} \quad \text{Normal Velocity}$$

$$\eta' = \tilde{\eta}(y)e^{i(\alpha x + \beta z - \omega t)} \quad \text{Vorticity}$$

Knowing that  $\alpha^2 + \beta^2 = k^2$ , and expressing the derivative in  $y$  as  $D$ , the equations for  $v'$  and for  $\eta'$  are:

$$\left[ (-i\omega + i\alpha U)(D^2 - k^2) - i\alpha \frac{\partial^2 U}{\partial y^2} - \frac{1}{Re}(D^2 - k^2)^2 \right] \tilde{v} = 0$$

$$\left[ \left( -i\omega + i\alpha U - \frac{1}{Re} \right) (D^2 - k^2) \right] \tilde{\eta} = -i\beta \frac{\partial U}{\partial y} \tilde{v}$$

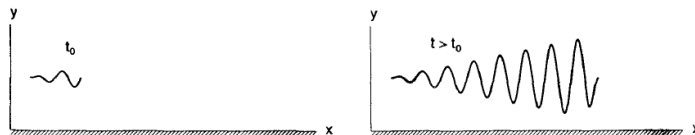
Orr - Sommerfeld Equation

Squire Equation

Spatial Analysis

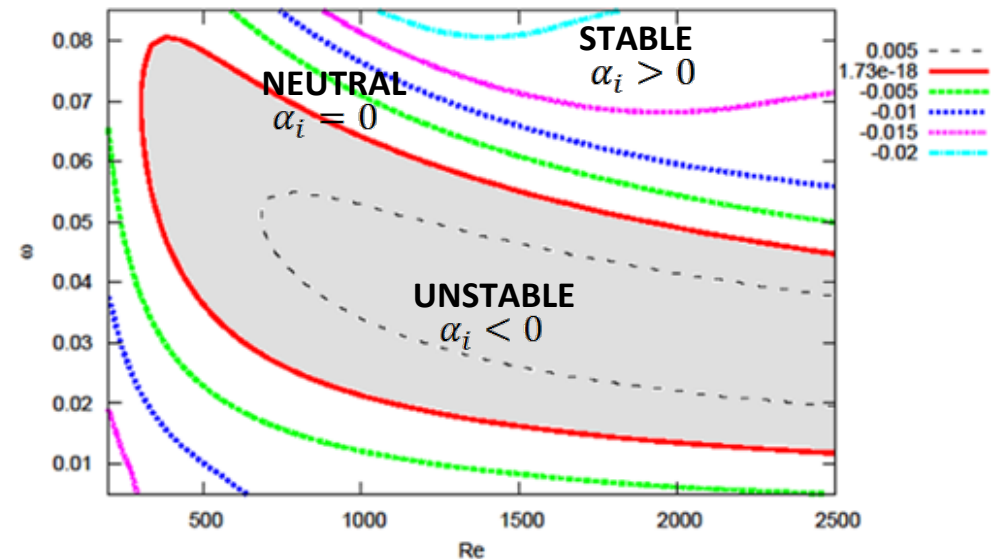
$$\omega, \beta \in \mathbb{R}$$

$$\alpha \in \mathbb{C}$$



Perturbation velocity:

$$V' = V(y)e^{i(\alpha_r x + \beta z - \omega t)} e^{-\alpha_i x}$$





# THEORY

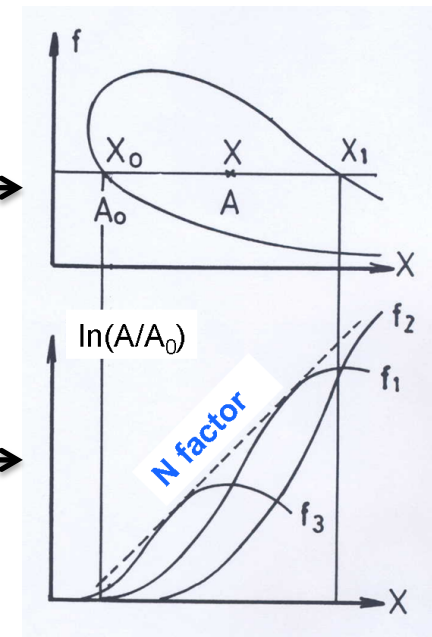
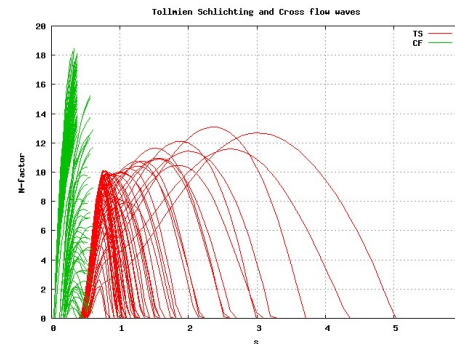
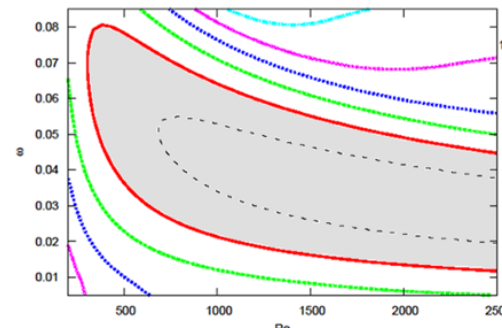
At a given station, the **total amplification rate** of a spatially growing wave can be defined as:

$$\ln(A/A_0) = \int_{x_0}^x -\alpha_i(x) dx$$

- A = wave amplitude
- $A_0 = X_0$  position (where the wave begins to be unstable)

The **envelope** of the total amplification curves is:

$$N = \max_f [\ln(A/A_0)]$$





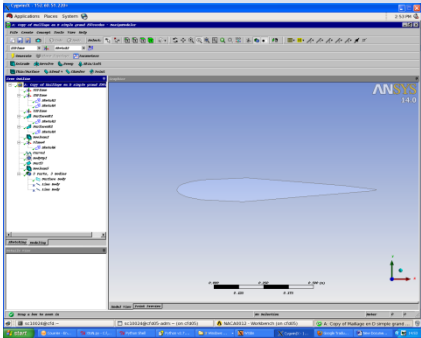
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# **METHODOLOGY DEVELOPED**

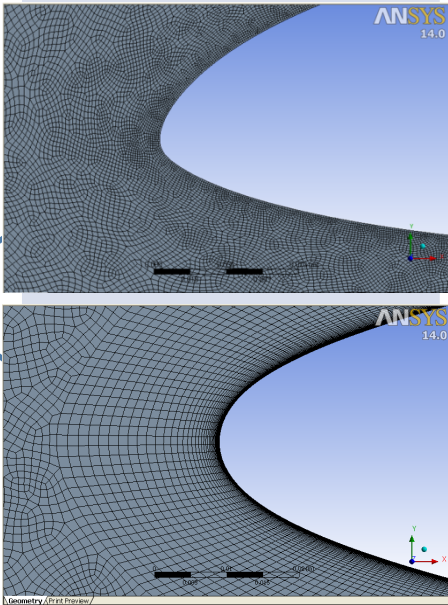
# METHODOLOGY DEVELOPED



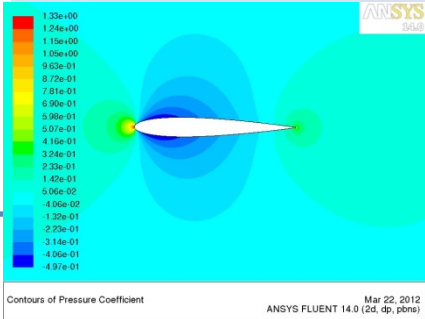
## WING PROFILE



## MESH

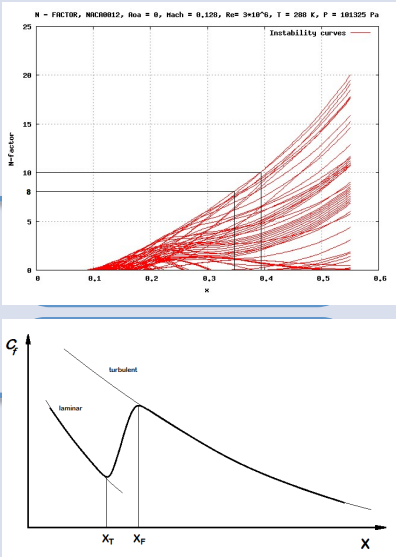


## RESULTS



**Fluent**  
SST-TRANSITION  
MODEL

## POST-PROCESS





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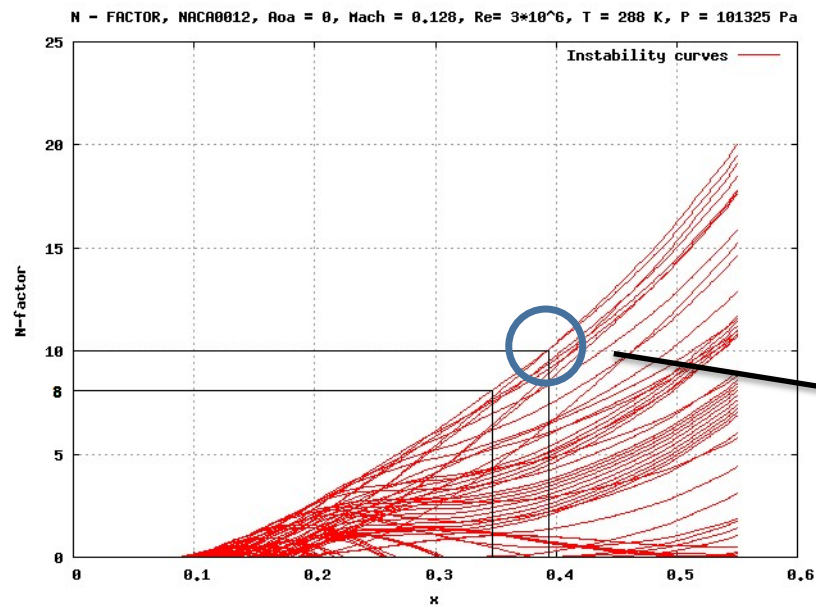
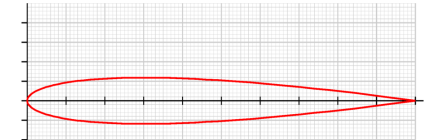
# TEST CASES 2D

# TEST CASES (2D)



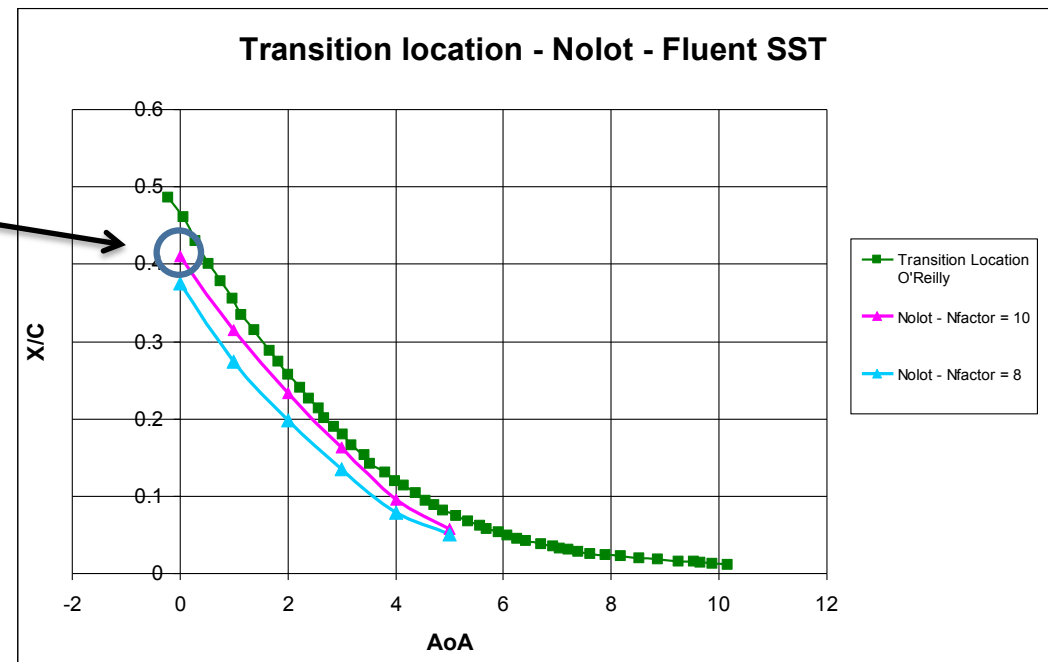
## NACA0012

Mach = 0.128, T = 288.15 K, P = 101325 Pa, Re =  $3 \times 10^6$



← N-factor plot, amplification rate for AoA = 0°

EXPERTIMENTS vs Nolot →

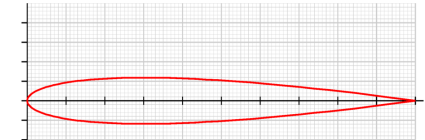


# TEST CASES (2D)



## NACA0012

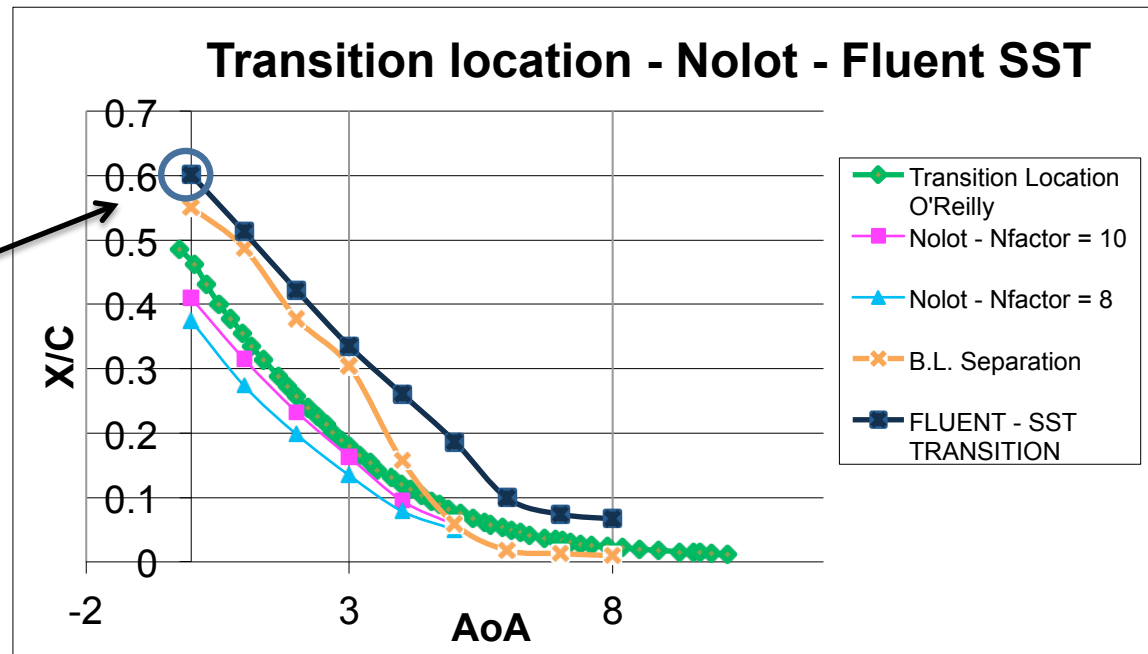
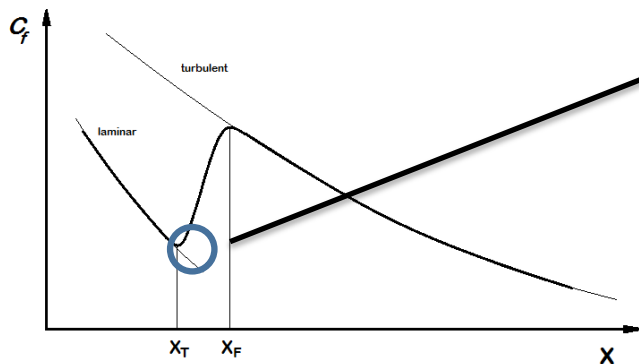
Mach = 0.128, T = 288.15 K, P = 101325 Pa, Re =  $3 \times 10^6$



### Viscous Calculation

Transition location in **viscous case** -> Cf

**Rapid growth** -> switch from laminar to turbulent

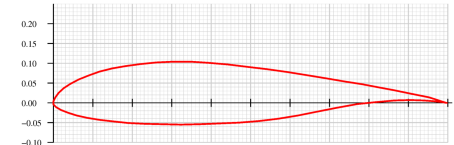


# TEST CASES (2D)



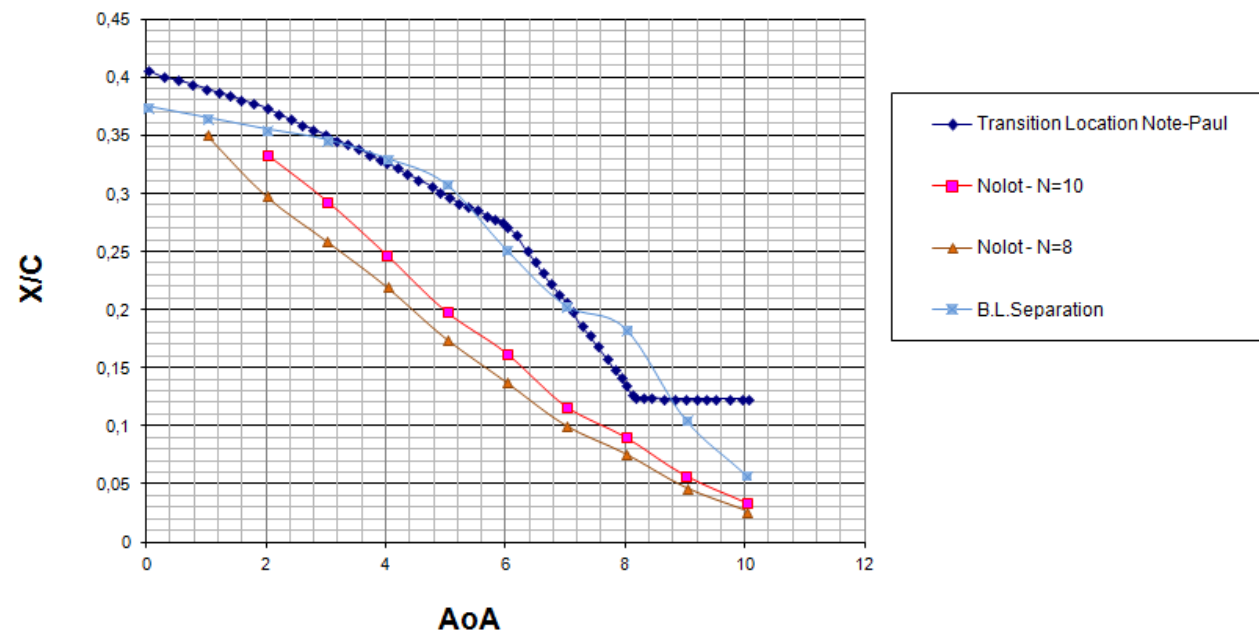
## NLF0416

Mach = 0.1, T = 288.15 K, P = 101325 Pa, Re =  $4 \times 10^6$



Transition location in the article (“Transition-Flow-Occurrence-Estimation “A New Method” by Paul-Dan Silisteanu and Ruxandra M. Botez ) is actually the the separation location.

Experimental and Theoretical Transition Location







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# TEST CASE 3D

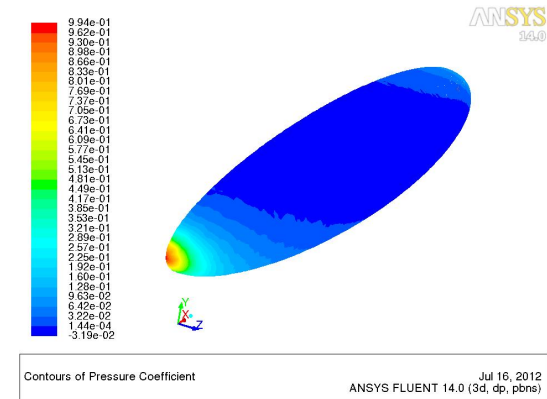
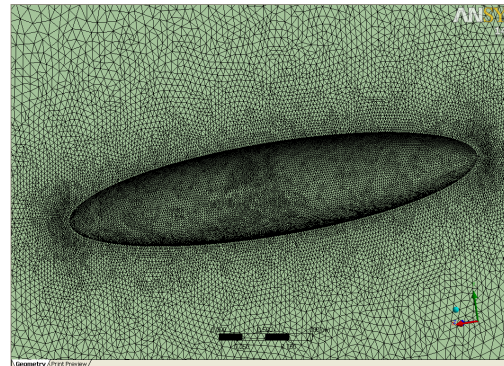


# TEST CASE (3D)

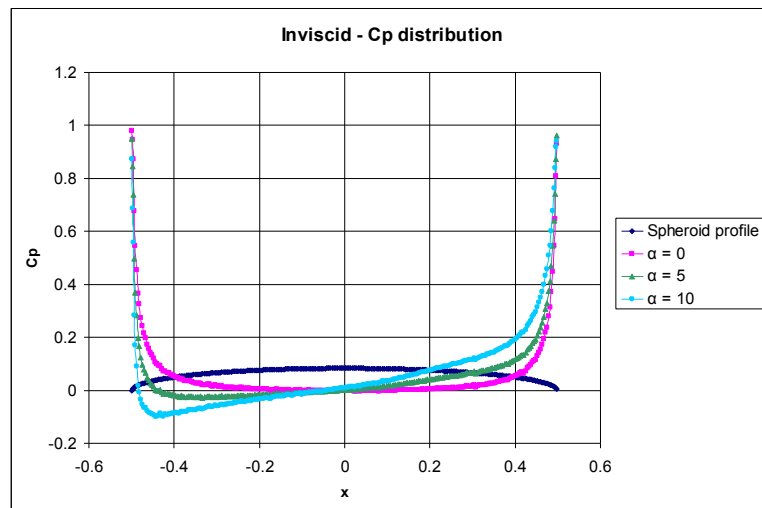
## SPHEROID

**MESH** and **PRESSURE DISTRIBUTION**  
on the spheroid  
(for inviscid calculation):

Mach = 0.3, T = 281.53 K, P = 101325 Pa, Re =  $7.2 \times 10^6$



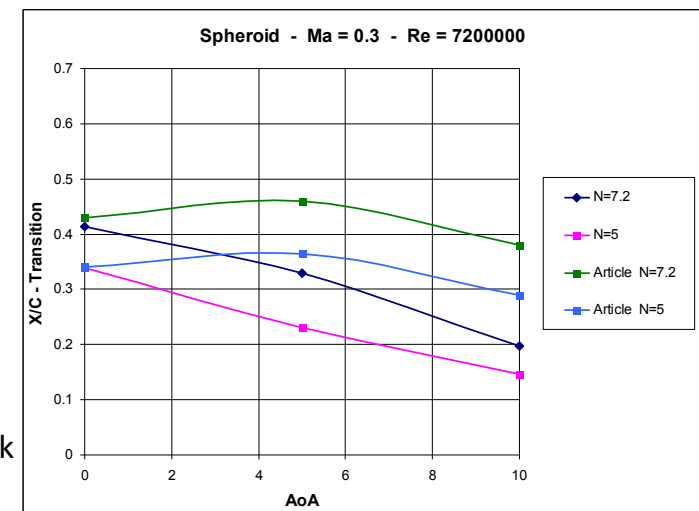
Cp distribution on the symmetry plane for:  
AoA = 0°  
AoA = 5°  
AoA = 10°



**Nolot Transition location VS Experiments**



Only AoA = 0° case → ok

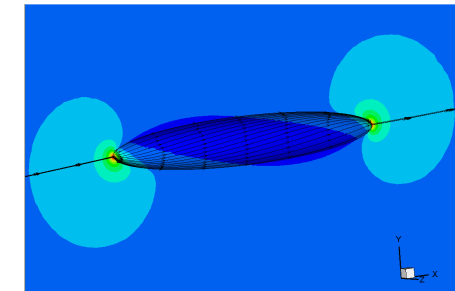
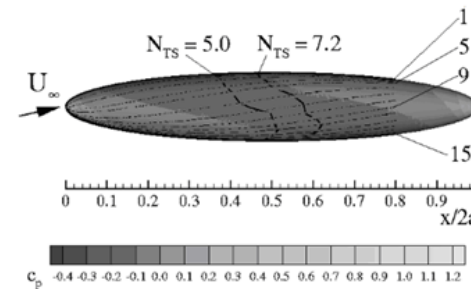




# TEST CASE (3D)

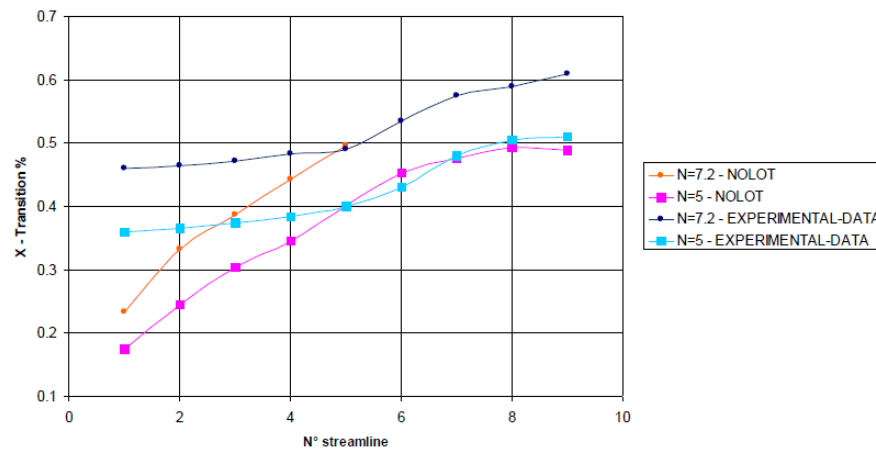
## SPHEROID

- **NEW IDEA** → study along the streamlines
- **No crossflow** → two-dimensional analysis



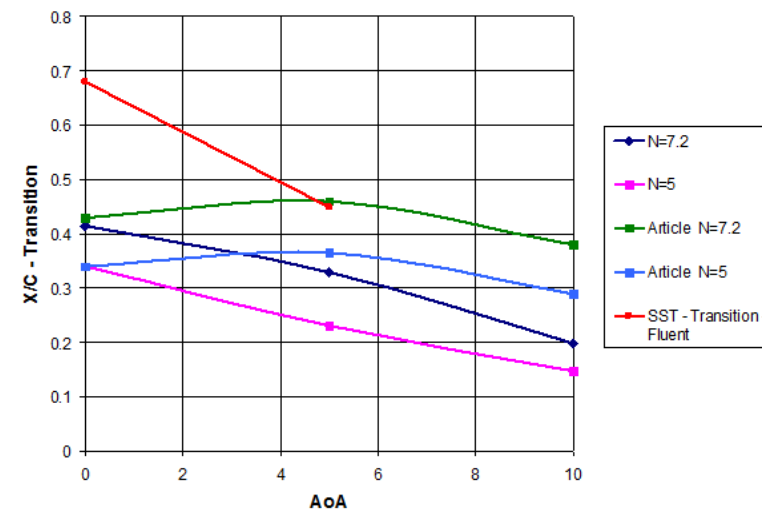
### Results of the analysis ALONG THE STREAMLINES:

Far from the symmetry plane → Nolut ok  
 For N=7.2 → Nolut not ok



### VISCOUS CALCULATION:

AoA = 10° → no convergence  
 AoA = 5° → Fluent ok  
 AoA = 0° → Fluent **not** ok



# CONCLUSIONS



- A **methodology** to predict transition based on physical mechanisms has been **implemented and verified** in an industrial fluid solver (software)
- **Validation** is **successful** for **2D** profiles, as **NACA0012**.
- For the **NLF0416 profile** we **cannot be sure** of the results since the literature provide us only the boundary layer separation.
- **Validation** for the **3D geometries** is more complicated for 3D effects.
- **Same methodology along the streamlines** is ok but far from the symmetry plain.
- For the moment **Nolot code** works only on **simple geometries** like a spheroid (**axisymmetric**), infinite swept wings.

# FUTURE WORK

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- **Manage** the entire **methodology** to make it **faster, efficient** and **reliable**.
- Make a study of the **entire spheroid** to see **how much the symmetry plane influences the flow** close to it.
- Improving the **Nolot** code to use it **along the streamlines** allows to extend the methodology from 2D to 3D geometries.



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**THANKS FOR THE ATTENTION**